- 1. Consider the curves $r = 3\cos(\theta)$ and $r = 1 + \cos(\theta)$
- a) Sketch the curves on the same set of axes using the polar axes below



b) Find the area of the region inside the curve $r = 3\cos(\theta)$ and outside the curve $r = 1 + \cos(\theta)$ by setting up and evaluating a definite integral. Your work must include an antiderivative.

- 2. A particle moves along a curve given parametrically by $x = 3 2\cos(3t)$ and $y = 1 + 4\sin(3t)$.
 - a) Give a sketch of the parametric curve including the direction of motion based on the equation you get by eliminating parameter t.
 - b) A range of t for a single trace of the curve
 - c) The equation of the line tangent to the path of the particle at t = $\pi/18$.
 - d) The concavity of the curve at t = $\pi/18$.
- 3. Determine the length of the curve given by $y = 7(6+x)^{3/2}$ for $189 \le y \le 875$
- 4. Evaluate each of the following integrals:

a)
$$\int 4x \cos(2-3x) dx$$

b) $\int_{6}^{0} (2+5x) e^{x/3} dx$
c) $\int \sin^{3} \left(\frac{2x}{3}\right) \cos^{4} \left(\frac{2x}{3}\right) dx$
d) $\int \frac{\sqrt{x^{2}+16}}{x^{4}} dx$
e) $\int \frac{8-3t}{10t^{2}+13t-3} dx$

- 5. Determine the area of the region bounded by $y = xe^{-x^2}$, y = x + 1, x = 2 and the y axis.
- 6. Determine the volume of the solid obtained by rotating the region bounded by $y = (x 1)(x 3)^2$ and the x-axis about the y-axis.
- 7. Evaluate the following limits:

a)
$$\lim_{t \to 4} \frac{t - \sqrt{3t + 4}}{4 - t}$$

b)
$$\lim_{t \to \infty} \frac{4 + 7t}{2 - t}$$

c)
$$\lim_{t \to 0^+} \sin(t)^{\tan(t)}$$

- 8. An airline requires the total outside dimensions (length + width + height) of a checked bag not to exceed 62 inches. Suppose you want to check a bag whose height is equal to its width. What is the largest volume of a bag of this shape that will meet the criteria?
- 9. Find the maxima/minima (if it/they exist) for the function $y = \frac{x}{1 + x^2}$
- 10. Calculate the equation(s) of the line(s) tangent to the curve $x^3y^2 + 2xy + 5x^2 = 8$ at the point where x = 1.